

8 Rearrange this equation to make x the subject.

$$y = 7x + 2$$

$$y = 7x + 2$$

-2 -2

$$y - 2 = 7x$$

$\div 7$ $\div 7$

$$\frac{y - 2}{7} = x$$

$$x = \frac{y - 2}{7} \quad [2]$$

7 Make x the subject of this formula.

$$2y = 5x - 7$$

$$2y = 5x - 7$$

$+7$ $+7$

$$2y + 7 = 5x$$

$\div 5$ $\div 5$

$$\frac{2y + 7}{5} = x$$

$$x = \frac{2y + 7}{5} \quad [2]$$

11

$$y = \frac{w^2}{2}$$

Rearrange the formula to make w the subject.

$$y = \frac{w^2}{2}$$

$\times 2$ $\times 2$

$$2y = w^2$$

$\sqrt{\quad}$ $\sqrt{\quad}$

$$\sqrt{2y} = w$$

$$w = \sqrt{2y} \quad [1]$$

8 $s = \frac{1}{2}at^2$

(a) Work out the value of s when $a = 0.9$ and $t = 4$.

$$s = \frac{1}{2}(0.9) \times 4^2$$

$$= 7.2$$

$s = \dots 7.2 \dots$ [1]

(b) Rearrange the formula to find t in terms of s and a .

$$s = \frac{at^2}{2}$$

$$2s = at^2$$

$$\frac{2s}{a} = t^2$$

$$\sqrt{\frac{2s}{a}} = t$$

$t = \dots \sqrt{\frac{2s}{a}} \dots$ [2]

19 Make y the subject of the formula.

$$h^2 = x^2 + 2y^2$$

$$h^2 = x^2 + 2y^2$$

$$h^2 - x^2 = 2y^2$$

$$\frac{h^2 - x^2}{2} = y^2$$

$$\sqrt{\frac{h^2 - x^2}{2}} = y$$

$y = \dots \sqrt{\frac{h^2 - x^2}{2}} \dots$ [3]

10 Rearrange the formula to make x the subject.

$$y(x+4) = 2$$

$$y(x+4) = 2$$

$$xy + 4y = 2$$

$$xy = 2 - 4y$$

$$x = \frac{2 - 4y}{y}$$

$x = \dots \frac{2 - 4y}{y} \dots$ [2]

12 Rearrange this formula to make R the subject.

$$P = \frac{2(Q+3R)}{5}$$

$$P = \frac{2Q + 6R}{5}$$

$$5P = 2Q + 6R$$

$$5P - 2Q = 6R$$

$$\frac{5P - 2Q}{6} = R$$

$$R = \frac{5P - 2Q}{6} \quad [3]$$

8 $A = 2\pi rh + 3\pi r^2$

Rearrange the formula to write h in terms of π , r and A .

$$A = 2\pi rh + 3\pi r^2$$

$$A - 3\pi r^2 = 2\pi rh$$

$$\frac{A - 3\pi r^2}{2\pi r} = h$$

$$h = \frac{A - 3\pi r^2}{2\pi r} \quad [2]$$

14 $y = 2w^2 - x$

Rearrange the formula to make w the subject.

$$y = 2w^2 - x$$

$$y + x = 2w^2$$

$$\frac{y + x}{2} = w^2$$

$$\sqrt{\frac{y + x}{2}} = w$$

$$w = \sqrt{\frac{y + x}{2}} \quad [3]$$

7 $J = h^3 + k^3$

(a) Find the value of J when $h = 3$ and $k = 4$.

$$J = 3^3 + 4^3$$

$$= 91$$

$J = \dots 91 \dots$ [2]

(b) Rearrange the formula to write h in terms of J and k .

$$J = h^3 + k^3$$

$$J - k^3 = h^3$$

$$\sqrt[3]{J - k^3} = h$$

$h = \dots \sqrt[3]{J - k^3} \dots$ [2]

10 $J = m(k^2 + h^2)$

Rearrange the formula to make h the subject.

$$J = mk^2 + mh^2$$

$$J - mk^2 = mh^2$$

$$\frac{J - mk^2}{m} = h^2$$

$$h = \sqrt{\frac{J - mk^2}{m}}$$

$h = \dots \sqrt{\frac{J - mk^2}{m}} \dots$ [3]

11 $P = M(g^2 + h^2)$

(a) Find the value of P when $M = 100$, $g = 3$ and $h = 4.5$.

$$P = 100(3^2 + 4.5^2)$$

$$= 2925$$

$P = \dots 2925 \dots$ [2]

(b) Rearrange the formula to write g in terms of P , M and h .

$$P = Mg^2 + Mh^2$$

$$P - Mh^2 = Mg^2$$

$$\frac{P - Mh^2}{M} = g^2$$

$$\sqrt{\frac{P - Mh^2}{M}} = g$$

$g = \dots \sqrt{\frac{P - Mh^2}{M}} \dots$ [3]

15 $y = \sqrt{u^2x}$

(a) Find the value of y when $u = 7$ and $x = 25$.

$$y = \sqrt{7^2 \times 25}$$

$$= 35$$

$y = \dots 35 \dots$ [2]

(b) Rearrange the formula to write x in terms of u and y .

$$y = \sqrt{u^2x}$$

$$y^2 = u^2x$$

$$\frac{y^2}{u^2} = x$$

$x = \dots \frac{y^2}{u^2} \dots$ [2]

15 $T = \sqrt{3d - e}$

Rearrange the formula to make d the subject.

$$\begin{aligned}
 T &= \sqrt{3d - e} \\
 \text{sq.} \quad \text{sq.} \\
 T^2 &= 3d - e \\
 +e \quad +e \\
 T^2 + e &= 3d \\
 \div 3 \quad \div 3 &
 \end{aligned}
 \qquad
 \begin{aligned}
 &\rightarrow \frac{T^2 + e}{3} = d \\
 d &= \frac{T^2 + e}{3} \quad [3]
 \end{aligned}$$

10 Rearrange the formula to write x in terms of a and y .

$$\begin{aligned}
 y &= \sqrt{x^2 + 2a^2} \\
 \text{sq.} \quad \text{sq.} \\
 y^2 &= x^2 + 2a^2 \\
 -2a^2 \quad -2a^2 \\
 y^2 - 2a^2 &= x^2 \\
 \sqrt{y^2 - 2a^2} &= x \\
 x &= \sqrt{y^2 - 2a^2} \quad [3]
 \end{aligned}$$

15 $m = 2p + \sqrt{\frac{x}{y}}$

Make x the subject of this formula.

$$\begin{aligned}
 m &= 2p + \sqrt{\frac{x}{y}} \\
 -2p \quad -2p \\
 m - 2p &= \sqrt{\frac{x}{y}} \\
 \text{sq.} \quad \text{sq.} \\
 (m - 2p)^2 &= \frac{x}{y} \\
 \times y \quad \times y &
 \end{aligned}
 \qquad
 \begin{aligned}
 &\rightarrow y(m - 2p)^2 = x \\
 x &= y(m - 2p)^2 \quad [3]
 \end{aligned}$$

15 Rearrange the equation to make x the subject.

$$A + 4y = A(2 - 3x)$$

$$\begin{aligned}
 A + 4y &= 2A - 3Ax \\
 + 3Ax & \quad + 3Ax \\
 3Ax + A + 4y &= 2A \\
 -A & \quad -A \\
 3Ax + 4y &= A \\
 -4y & \quad -4y \\
 3Ax &= A - 4y \\
 \div 3A & \quad \div 3A
 \end{aligned}
 \rightarrow x = \frac{A - 4y}{3A}$$

$$x = \frac{A - 4y}{3A} \dots \dots \dots [3]$$

(b) Rearrange the formula $V = 2x^3 - 3y^3$ to make y the subject.

$$\begin{aligned}
 V &= 2x^3 - 3y^3 \\
 + 3y^3 & \quad + 3y^3 \\
 V + 3y^3 &= 2x^3 \\
 -V & \quad -V \\
 3y^3 &= 2x^3 - V \\
 \div 3 & \quad \div 3
 \end{aligned}
 \rightarrow y^3 = \frac{2x^3 - V}{3}$$

$$y = \sqrt[3]{\frac{2x^3 - V}{3}}$$

$$y = \frac{\sqrt[3]{2x^3 - V}}{3} \dots \dots \dots [3]$$

14 $A = P(1+x)^3$

Rearrange the formula to write x in terms of A and P .

$$\begin{aligned}
 A &= P(1+x)^3 \\
 \div P & \quad \div P \\
 \frac{A}{P} &= (1+x)^3 \\
 \sqrt[3]{\frac{A}{P}} & \quad \sqrt[3]{} \\
 \sqrt[3]{\frac{A}{P}} &= 1+x \\
 -1 & \quad -1
 \end{aligned}
 \rightarrow \sqrt[3]{\frac{A}{P}} - 1 = x$$

$$x = \sqrt[3]{\frac{A}{P}} - 1 \dots \dots \dots [3]$$

11 $y = \frac{2}{x+3}$

Rearrange the formula to make x the subject.

$$\begin{aligned}
 y &= \frac{2}{x+3} \\
 y(x+3) &= 2 \\
 xy + 3y &= 2 \\
 xy &= 2 - 3y \\
 x &= \frac{2-3y}{y} \quad [3]
 \end{aligned}$$

(d) Make x the subject of the formula.

$$x = \frac{3+x}{y}$$

$$\begin{aligned}
 x &= \frac{3+x}{y} \\
 xy &= 3+x \\
 xy - x &= 3 \\
 x(y-1) &= 3 \\
 x &= \frac{3}{y-1} \quad [3]
 \end{aligned}$$

14 Make x the subject of $A = \frac{3(x+y)}{x}$.

$$A = \frac{3x + 3y}{x}$$

$$Ax = 3x + 3y$$

$$Ax - 3x = 3y$$

$$x(A - 3) = 3y$$

$$x = \frac{3y}{A - 3}$$

$$x = \frac{3y}{A - 3} \quad [3]$$

18 Make x the subject of the formula.

$$c = \frac{3x}{2x - 5}$$

$$c = \frac{3x}{2x - 5}$$

$$c(2x - 5) = 3x$$

$$2cx - 5c = 3x$$

$$2cx = 3x + 5c$$

$$2cx - 3x = 5c$$

$$x(2c - 3) = 5c$$

$$x = \frac{5c}{2c - 3} \quad [4]$$

17 Rearrange the formula to make m the subject.

$$R = \frac{2(m - k)}{m}$$

$$R = \frac{2m - 2k}{m}$$

$$mR = 2m - 2k$$

$$mR - 2m = -2k$$

$$m(R - 2) = -2k$$

$$m = \frac{-2k}{R - 2}$$

$$m = \frac{-2k}{R - 2} \quad [4]$$

14 Make x the subject of the formula.

$$\frac{p}{x} = \frac{q}{x-2}$$

$$p(x-2) = qx$$

$$px - 2p = qx$$

$$+ 2p \quad + 2p$$

$$px = qx + 2p$$

$$-qx \quad -qx$$

$$px - qx = 2p$$

$$x(p-q) = 2p$$

$$\div (p-q) \quad \div (p-q)$$

$$x = \frac{2p}{p-q}$$

$$x = \frac{2p}{p-q} \quad [3]$$

12 Rearrange this formula to make x the subject.

$$y = \frac{a-x}{3x}$$

$$y = \frac{a-x}{3x}$$

$$\times 3x$$

$$\times 3x$$

$$3xy = a - x$$

$$+x$$

$$+x$$

$$3xy + x = a$$

$$x(3y+1) = a$$

$$\div (3y+1)$$

$$\div (3y+1)$$

$$x = \frac{a}{3y+1}$$

$$x = \frac{a}{3y+1} \quad [3]$$

15 Make h the subject of the formula $2mh = g(1-h)$.

$$2mh = g - gh$$

$$+gh$$

$$+gh$$

$$2mh + gh = g$$

$$h(2m+g) = g$$

$$\div (2m+g)$$

$$\div (2m+g)$$

$$h = \frac{g}{2m+g}$$

$$h = \frac{g}{2m+g} \quad [4]$$

(e) Make x the subject of the formula.

$$y = \frac{5(p-2x)}{x}$$

$$y = \frac{5p - 10x}{x}$$

$$xy = 5p - 10x$$

$$xy + 10x = 5p$$

$$x(y+10) = 5p$$

$$x = \frac{5p}{y+10}$$

$$x = \frac{5p}{y+10} \quad [4]$$

18 Make t the subject of the formula.

$$2 = \frac{m(1-t)}{pt}$$

$$2 = \frac{m - mt}{pt}$$

$$2pt = m - mt$$

$$2pt + mt = m$$

$$t(2p+m) = m$$

$$t = \frac{m}{2p+m}$$

$$t = \frac{m}{2p+m} \quad [4]$$

17 $y = \frac{3x-2}{1-x}$

Make x the subject of the formula.

$$y = \frac{3x-2}{1-x}$$

$\times (1-x)$ $\times (1-x)$

$$y(1-x) = 3x-2$$

$$y - xy = 3x-2$$

$+xy$ $+xy$

$$y = 3x + xy - 2$$

$+2$ $+2$

$$y+2 = 3x+xy$$

$$y+2 = x(3+y)$$

$\div (3+y)$ $\div (3+y)$

$$\frac{y+2}{3+y} = x$$

$$x = \frac{y+2}{3+y} \quad [4]$$

9 Rearrange this equation to make x the subject.

$$\frac{a}{2x-3} = \frac{b}{5x}$$

$$5ax = b(2x-3)$$

$$5ax = 2bx - 3b$$

$-2bx$ $-2bx$

$$5ax - 2bx = -3b$$

$$x(5a - 2b) = -3b$$

$\div (5a-2b)$ $\div (5a-2b)$

$$x = \frac{-3b}{5a-2b}$$

$$x = \frac{-3b}{5a-2b} \quad [3]$$