

- 4 A cyclist starts from rest at a point A and travels along a straight road AB , coming to rest at B . The displacement of the cyclist from A at time t s after the start is s m, where

$$s = 0.004(75t^2 - t^3).$$

- (a) Show that the distance AB is 250 m.

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- (b) Find the maximum velocity of the cyclist.

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- 6** A particle moves in a straight line AB . The velocity $v \text{ m s}^{-1}$ of the particle $t \text{ s}$ after leaving A is given by $v = k(t^2 - 10t + 21)$, where k is a constant. The displacement of the particle from A , in the direction towards B , is 2.85 m when $t = 3$ and is 2.4 m when $t = 6$.
- (a)** Find the value of k . Hence find an expression, in terms of t , for the displacement of the particle from A . [7]

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- (b) Find the displacement of the particle from A when its velocity is a minimum. [4]

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- 6 A particle travels in a straight line PQ . The velocity of the particle t s after leaving P is $v \text{ m s}^{-1}$, where

$$v = 4.5 + 4t - 0.5t^2.$$

- (a) Find the velocity of the particle at the instant when its acceleration is zero. [3]

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[6]

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- 5** A particle moving in a straight line starts from rest at a point A and comes instantaneously to rest at a point B . The acceleration of the particle at time t s after leaving A is $a \text{ m s}^{-2}$, where

$$a = 6t^{\frac{1}{2}} - 2t.$$

- (a) Find the value of t at point B . [3]

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- (b) Find the distance travelled from A to the point at which the acceleration of the particle is again zero. [5]

This image shows a full page of white paper with horizontal dotted lines, typical of primary school writing paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- 7 A particle P travels in a straight line, starting at rest from a point O . The acceleration of P at time t s after leaving O is denoted by $a \text{ m s}^{-2}$, where

$$\begin{aligned} a &= 0.3t^{\frac{1}{2}} & \text{for } 0 \leq t \leq 4, \\ a &= -kt^{-\frac{3}{2}} & \text{for } 4 < t \leq T, \end{aligned}$$

where k and T are constants.

- (a) Find the velocity of P at $t = 4$. [2]

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- (b) It is given that there is no change in the velocity of P at $t = 4$ and that the velocity of P at $t = 16$ is 0.3 m s^{-1} .

Show that $k = 2.6$ and find an expression, in terms of t , for the velocity of P for $4 \leq t \leq T$. [4]

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(d) Find the total distance travelled between $t = 0$ and $t = T$. [4]

[illegible]

- 3** A particle moves in a straight line starting from rest from a point O . The acceleration of the particle at time t s after leaving O is $a \text{ m s}^{-2}$, where $a = 4t^{\frac{1}{2}}$.

(a) Find the speed of the particle when $t = 9$. [2]

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(b) Find the time after leaving O at which the speed (in metres per second) and the distance travelled (in metres) are numerically equal. [3]

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- 5** A particle P moves in a straight line. It starts at a point O on the line and at time t s after leaving O it has velocity $v \text{ m s}^{-1}$, where $v = 4t^2 - 20t + 21$.

(a) Find the values of t for which P is at instantaneous rest. [2]

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(b) Find the initial acceleration of P . [2]

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(c) Find the minimum velocity of P . [2]

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- 6 A particle starts from a point O and moves in a straight line. The velocity $v \text{ m s}^{-1}$ of the particle at time $t \text{ s}$ after leaving O is given by

$$v = k(3t^2 - 2t^3),$$

where k is a constant.

- (a) Verify that the particle returns to O when $t = 2$. [4]

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- 6** A cyclist starts from rest at a fixed point O and moves in a straight line, before coming to rest k seconds later. The acceleration of the cyclist at time t s after leaving O is $a \text{ m s}^{-2}$, where $a = 2t^{-\frac{1}{2}} - \frac{3}{5}t^{\frac{1}{2}}$ for $0 < t \leq k$.

(a) Find the value of k .

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(b) Find the maximum speed of the cyclist.

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- (c) Find an expression for the displacement from O in terms of t . Hence find the total distance travelled by the cyclist from the time at which she reaches her maximum speed until she comes to rest. [4]

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- 7 A particle moves in a straight line through the point O . The displacement of the particle from O at time t s is s m, where

$$s = t^2 - 3t + 2 \quad \text{for } 0 \leq t \leq 6,$$

$$s = \frac{24}{t} - \frac{t^2}{4} + 25 \quad \text{for } t \geq 6.$$

- (a) Find the value of t when the particle is instantaneously at rest during the first 6 seconds of its motion. [2]

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At $t = 6$, the particle hits a barrier at a point P and rebounds.

- (b) Find the velocity with which the particle arrives at P and also the velocity with which the particle leaves P . [3]

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This image shows a full page of white paper with horizontal dotted lines, typical of primary school writing paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- 6 A particle P moves in a straight line starting from a point O and comes to rest 14 s later. At time t s after leaving O , the velocity v m s⁻¹ of P is given by

$$\begin{aligned} v &= pt^2 - qt & 0 \leq t \leq 6, \\ v &= 63 - 4.5t & 6 \leq t \leq 14, \end{aligned}$$

where p and q are positive constants.

The acceleration of P is zero when $t = 2$.

- (a) Given that there are no instantaneous changes in velocity, find p and q . [3]

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- (b) Sketch the velocity-time graph. [3]

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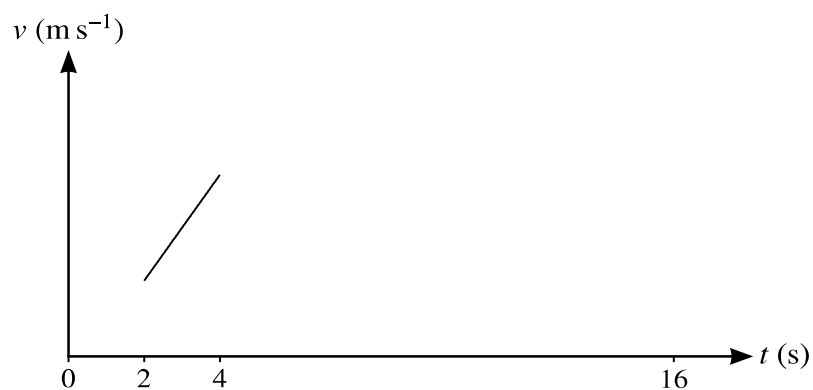
- 7 A particle P moving in a straight line starts from rest at a point O and comes to rest 16 s later. At time t s after leaving O , the acceleration $a \text{ m s}^{-2}$ of P is given by

$$\begin{array}{ll} a = 6 + 4t & 0 \leq t < 2, \\ a = 14 & 2 \leq t < 4, \\ a = 16 - 2t & 4 \leq t \leq 16. \end{array}$$

There is no sudden change in velocity at any instant.

- (a) Find the values of t when the velocity of P is 55 m s^{-1} . [5]

This image shows a single page of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



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